

Calculer $\lim_{x \rightarrow \frac{\pi}{2}} (1 - \sin x) \cdot \tan x$.

On a :

$$\begin{aligned} \lim_{x \rightarrow \frac{\pi}{2}} (1 - \sin x) \cdot \tan x &\stackrel{(\text{FI})}{=} [0 \cdot \infty] \\ &= \lim_{x \rightarrow \frac{\pi}{2}} (1 - \sin x) \cdot \frac{\sin x}{\cos x} \\ &\stackrel{(\text{FI})}{=} \left[\frac{0}{0} \right] \\ &\stackrel{(\text{H})}{=} \lim_{x \rightarrow \frac{\pi}{2}} \frac{\cos x \cdot (1 - 2 \sin x)}{-\sin x} \\ &= \boxed{0} \end{aligned}$$