

Calculer  $\lim_{x \rightarrow 0} \frac{\pi \sin \pi x}{2x \cos \pi x}$ .

$$\lim_{x \rightarrow 0} \frac{\pi \sin \pi x}{2x \cos \pi x} = \left[ \frac{0}{0} \right]$$

$$\stackrel{(H)}{=} \lim_{x \rightarrow 0} \frac{\pi^2 \cos \pi x}{2 \cos \pi x - 2\pi x \sin \pi x}$$

$$= \boxed{\frac{\pi^2}{2}}$$