

# Correlation constants for liquids

Procedures to speed calculations for:

- Surface tensions
- Heat capacities
- Liquid densities
- Thermal conductivities

*Carl L. Yaws, Lamar University, and others\**

□ The correlation constants for liquids presented in this article are based on extensive, available, experimental data. These constants are easy to use in a tabular format for rapid engineering calculations by means of a hand calculator or a computer. Such constants may

be used in chemical-reaction engineering, thermodynamics, fluid flow, heat transfer, mass transfer and process design. Whereas this part of the series presents correlation data for liquids only, Part 22 contained correlation data for several gases.

## SURFACE TENSIONS OF LIQUIDS

*Joseph W. Miller, Jr., and Carl L. Yaws*

Surface-tension data are important in many chemical-process engineering applications, such as heat, mass and momentum transfer operations that involve process equipment such as heat exchangers, distillation columns, absorption, and fluid-flow piping.

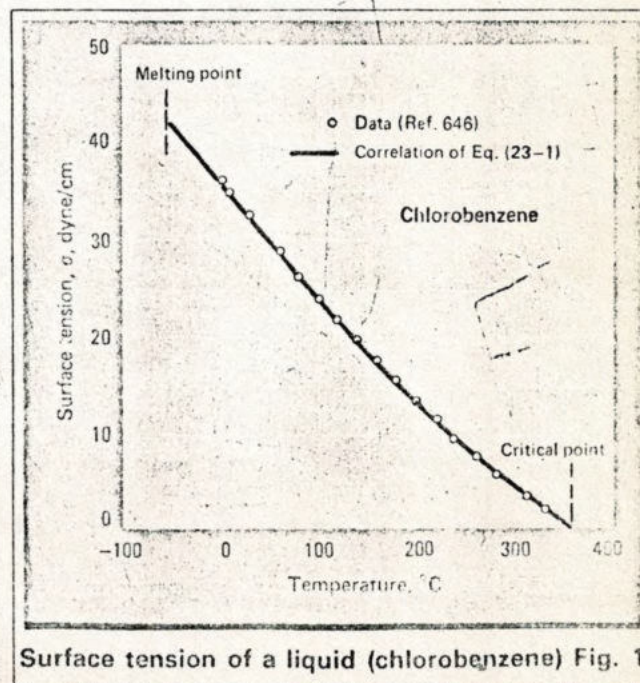
### Correlation constants—Table 23—I

Correlation constants for surface tension are based on the Othmer relation:

$$\sigma = \sigma_1 \left[ \frac{T_c - T}{T_c - T_1} \right]^n \quad (23-1)$$

where  $\sigma_1$  = surface tension at  $T_1$ , dynes/cm;  $T_c$  = critical temperature, K;  $T$  = temperature, K; and  $n$  = correlation parameter.

Tabulated values for the correlation constants are given in Table 23—I, where the temperature range of application is also presented. Deviations between data and calculated values were minimized by using a generalized least-squares computer program to ascertain



Surface tension of a liquid (chlorobenzene) Fig. 1

\*For author biographies, see p. 135

Correlation constants: surface tensions

Table 23-1

Compound	$\sigma = \sigma_1 \left[ \frac{T_c - T}{T_c - T_1} \right]^n$ , dynes/cm				Range, °C	References
	$\sigma_1$ , dynes/cm	$T_1$ , °C	$T_c$ , °C	$n$		
<b>Halogens</b>						
Fluorine, F <sub>2</sub>	16.82	-200.0	-129.0	0.8811	-219.6 to -129.0	31,69,79,637,646
Chlorine, Cl <sub>2</sub>	10.4	20.0	144.0	1.0503	-101.0 to 144.0	2,69,33,43,61,79,416
Bromine, Br <sub>2</sub>	41.5	20.0	315.0	1.1715	-7.2 to 315.0	2,6,9,43,63,79,416
Iodine, I <sub>2</sub>	36.8	125.0	546.0	1.1145	113.6 to 546.0	50
<b>Sulfur oxides</b>						
Sulfur dioxide, SO <sub>2</sub>	20.6	30.0	157.6	1.1768	-72.7 to 157.6	79,92,637
Sulfur trioxide, SO <sub>3</sub>	30.3	35.3	218.3	1.1854	16.8 to 218.3	6
<b>Nitrogen oxides</b>						
Nitrous oxide, N <sub>2</sub> O	1.75	20.0	36.5	1.3115	-89.5 to 36.5	6,9,10,12,79,416,574
Nitric oxide, NO	23.83	-156.0	-93.1	1.5473	-163.8 to -93.1	79
Nitrogen dioxide, NO <sub>2</sub>	26.5	25.0	158.0	0.7627	-11.2 to 158.0	6,10,12
<b>Carbon oxides</b>						
Carbon monoxide, CO	9.8	-193.0	-140.1	1.1441	-191.5 to -140.1	2,6,79,416
Carbon dioxide, CO <sub>2</sub>	1.16	20.0	31.1	1.3015	-56.5 to 31.1	2,6,9,79,415,416
<b>Hydrogen halides</b>						
Hydrogen fluoride, HF	9.62	10.0	188.0	1.3675	-83.5 to 188.0	4,10,12,70,169
Hydrogen chloride, HCl	24.7	-93.0	51.5	1.0972	-114.2 to 51.5	4,10,12,168
Hydrogen bromide, HBr	27.65	-70.0	90.0	1.2153	-66.9 to 90.0	10,12,79,168
Hydrogen iodide, HI	27.1	-36.0	151.0	1.2824	-50.8 to 151.0	10,12,158
<b>Nitrogen hydrides</b>						
Ammonia, NH <sub>3</sub>	36.67	-45.0	132.4	1.1548	-77.74 to 132.4	2,6,12,53,79,416,637
Hydrazine, N <sub>2</sub> H <sub>4</sub>	66.39	25.0	380.0	1.7652	2.0 to 380.0	4,5,3,79,189,190,214,416,637
<b>Hydrogen oxides</b>						
Water, H <sub>2</sub> O	71.97	25.0	374.2	0.8105	0.0 to 100.0	4,6,9,12,79,238,246,249,250,416,574,637,646
Hydrogen peroxide, H <sub>2</sub> O <sub>2</sub>	58.91	100.0	374.2	1.1690	100.0 to 374.2	
	76.1	18.2	455.0	0.9141	-0.43 to 455.0	4,79,249,250,256,257,416
<b>Diatomic gases</b>						
Hydrogen, H <sub>2</sub>	2.41	-256.0	-240.2	1.1012	-259.4 to -240.2	9,47,79,265,280,293,307,333,335,416,574,646
Nitrogen, N <sub>2</sub>	10.5	-203.0	-146.8	1.2123	-203.9 to -146.8	9,47,79,310,332,416,574,646
Oxygen, O <sub>2</sub>	18.01	-202.0	-118.5	1.1933	-218.4 to -118.5	9,73,303,334,416,574,637
<b>Inert gases</b>						
Helium, He	0.2390	-270.0	-268.0	0.5428	-272.66 to -270.0	9,47,79,345,416,574
Neon, Ne	0.2390	-270.0	-268.0	1.0638	-270.0 to -268.0	
Argon, Ar	5.5	-243.16	-228.7	1.2393	-248.7 to -228.7	9,47,345,416,574,646
	12.84	-187.16	-122.4	1.2834	-189.3 to -122.4	9,47,79,310,342,345,382
<b>Olefins</b>						
Ethylene, C <sub>2</sub> H <sub>4</sub>	19.52	-120.0	9.9	1.2760	-169.2 to 9.9	4,79,246,646
Propylene, C <sub>3</sub> H <sub>6</sub>	19.98	-70.0	91.9	1.1797	-185.3 to 91.9	10,79,246
1-Butene, C <sub>4</sub> H <sub>8</sub>	17.84	-20.0	146.2	1.2337	-185.4 to 146.2	10,79,246
<b>Alkanes</b>						
Methane, CH <sub>4</sub>	15.026	-168.16	-82.6	1.3941	-182.6 to -82.6	10,47,79,417,646
Ethane, C <sub>2</sub> H <sub>6</sub>	21.16	-120.0	32.3	1.2060	-183.2 to 32.3	10,79,417,646
Propane, C <sub>3</sub> H <sub>8</sub>	22.0	-90.0	96.7	1.1982	-187.7 to 96.7	10,79,417
<b>Xylenes</b>						
<i>o</i> -Xylene, C <sub>6</sub> H <sub>4</sub> (CH <sub>3</sub> ) <sub>2</sub>	30.1	20	357.8	1.2111	-25.2 to 357.8	3,6,79,415,416,417,646
<i>m</i> -Xylene, C <sub>6</sub> H <sub>4</sub> (CH <sub>3</sub> ) <sub>2</sub>	28.9	20.0	343.8	1.2629	-47.9 to 343.8	3,6,9,79,415,416,417,574,646
<i>p</i> -Xylene, C <sub>6</sub> H <sub>4</sub> (CH <sub>3</sub> ) <sub>2</sub>	28.31	20.0	344.0	1.2182	13.3 to 344.0	3,6,9,79,415,416,417,574,646
<b>Aromatics</b>						
Benzene, C <sub>6</sub> H <sub>6</sub>	28.88	20.0	288.94	1.2243	5.53 to 288.94	3,4,79,416,417,495,637,646
Naphthalene, C <sub>10</sub> H <sub>8</sub>	28.8	127.0	475.02	1.3511	80.55 to 475.02	3,6,79,574,637
<b>Alkyl aromatics</b>						
Toluene, C <sub>6</sub> H <sub>5</sub> CH <sub>3</sub>	28.52	20.0	318.8	1.2364	-95.0 to 318.8	3,9,79,415,417,520,574,637,646
Ethylbenzene, C <sub>6</sub> H <sub>5</sub> C <sub>2</sub> H <sub>5</sub>	29.29	20.0	344.0	1.2461	-95.0 to 344.0	3,9,79,415,417,520,637
Cumene, C <sub>6</sub> H <sub>5</sub> CH(CH <sub>3</sub> ) <sub>2</sub>	28.21	20.0	360.0	1.2807	-96.0 to 360.0	3,9,79,415,417,520,637,646
<b>Benzene derivatives</b>						
Chlorobenzene, C <sub>6</sub> H <sub>5</sub> Cl	33.5	20.0	359.2	1.2276	-45.2 to 359.2	3,4,6,70,415,546,569,637,646
Aniline, C <sub>6</sub> H <sub>5</sub> NH <sub>2</sub>	42.9	20.0	426.0	1.1022	-6.15 to 426.0	3,6,79,415,546,549,637,646
Phenol, C <sub>6</sub> H <sub>5</sub> OH	37.13	60.0	420.0	1.0725	40.75 to 420.0	3,6,79,415,569,570,574
<b>Cycloalkanes</b>						
Cyclopropane, C <sub>3</sub> H <sub>6</sub>	13.25	10.0	124.9	1.3201	-127.42 to 124.9	14
Cyclobutane, C <sub>4</sub> H <sub>8</sub>	19.13	10.0	190.4	1.3209	-90.73 to 190.4	14
Cyclopentane, C <sub>5</sub> H <sub>10</sub>	22.61	20.0	238.5	1.3323	-93.88 to 238.5	3,4,14,79,416,417,537,646
Cyclohexane, C <sub>6</sub> H <sub>12</sub>	25.24	20.0	280.3	1.4246	6.55 to 280.3	3,4,14,79,415,417,574,637,646
<b>Olefin monomers</b>						
Isobutylene, C <sub>4</sub> H <sub>8</sub>	12.42	20.0	144.7	1.2095	-140.35 to 144.7	3,4,75,417,620
Styrene, C <sub>6</sub> H <sub>5</sub> CH=CH <sub>2</sub>	23.01	60.0	369.0	0.4826	-30.6 to 369.0	3,4,79,416,620,621,628

Correlation constants: surface tensions (continued)

Table 23-1

Compound	$\sigma_1$ , dynes/cm	$T_1$ , °C	$T_c$ , °C	$n$	Range, °C	References
<b>Diolefins</b>						
1,3 Butadiene, C <sub>4</sub> H <sub>6</sub>	11.1	40.0	152.0	1.2055	-4.41 to 152.0	3,14
Isoprene, C <sub>5</sub> H <sub>8</sub>	13.6	50.0	210.2	1.2262	-146.0 to 210.2	14
Chloroprene, C <sub>4</sub> H <sub>5</sub> Cl	18.4	50.0	261.7	1.2227	-130.0 to 261.7	14,79
<b>Organic oxides</b>						
Ethylene oxide, C <sub>2</sub> H <sub>4</sub> O	24.33	20.0	195.8	1.1509	-112.5 to 195.8	2,4,10,79,416,574,659
Propylene oxide, C <sub>3</sub> H <sub>7</sub> O	24.8	0.0	209.1	1.2186	-112.0 to 209.1	14
Butylene oxide, C <sub>4</sub> H <sub>8</sub> O	26.3	0.0	252.6	1.2201	-150.0 to 252.6	14
<b>Primary alcohols</b>						
Methanol, CH <sub>3</sub> OH	22.6	20.0	239.4	0.8115	-97.6 to 239.4	4,6,9,79,415,416,574,637,642,646
Ethanol, C <sub>2</sub> H <sub>5</sub> OH	22.8	20.0	243.1	0.8760	-114.1 to 243.1	4,6,9,79,415,456,574,637,646
<i>n</i> -Propanol, C <sub>3</sub> H <sub>7</sub> OH	23.71	20.0	263.6	0.7859	-126.2 to 263.6	4,6,9,79,415,416,574,637
<i>n</i> -Butanol, C <sub>4</sub> H <sub>9</sub> OH	24.7	20.0	269.8	0.8395	-89.3 to 269.8	6,9,79,415,416,495,574,637
<b>Chloromethanes</b>						
Methyl chloride, CH <sub>3</sub> Cl	16.2	20.0	143.1	1.2234	-97.7 to 143.1	4,6,9,79,416,574
Methylene chloride, CH <sub>2</sub> Cl <sub>2</sub>	28.0	20.0	241.0	1.2057	-96.7 to 241.0	4,6,415,416,637,708,717,721
Chloroform, CHCl <sub>3</sub>	26.67	25.0	263.4	1.1824	-63.2 to 263.4	4,6,9,79,415,416,574,637,708,717,721
Carbon tetrachloride, CCl <sub>4</sub>	25.7	30.0	283.2	1.2278	-22.9 to 283.2	4,6,9,79,415,574,637,646,708,717,721

the correlation constants. Average deviations are less than 1-2% in most cases. A comparison of calculated and data values is presented in Fig. 23-1 for a representative chemical.

*Example 23-1*—Estimate the surface tension of benzene (C<sub>6</sub>H<sub>6</sub>) at 80°C. The solution to this problem is made by substituting the correlation constants ( $\sigma_1 = 28.88$ ;  $T_1 = 20^\circ\text{C} = 293.16\text{ K}$ ;  $T_c = 288.94^\circ\text{C} = 562.1\text{ K}$ ;  $T = 80^\circ\text{C} = 353.16\text{ K}$ ; and  $n = 1.2243$ ) from Table 23-1 into Eq. 23-1:

$$\begin{aligned}\sigma &= \sigma_1 \left[ \frac{T_c - T}{T_c - T_1} \right]^n \\ &= 28.88 \left[ \frac{562.1 - 353.16}{562.1 - 293.16} \right]^{1.2243} \\ &= 21.2 \text{ dyne/cm}\end{aligned}$$

The calculated and data values compare favorably (21.2 versus 21.2).

## HEAT CAPACITIES OF LIQUIDS

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Liquid heat-capacity data are important in many process engineering applications. For example, specific heat values are required in liquid-phase chemical reactions (energy requirements for heating liquid reactants up to reaction temperature); in distillation (energy requirements for cooling products to lower temperature for shipment to customer); and in general design of heat exchangers.

### Correlation constants—Table 23-II

Correlation constants for liquid heat capacity are based on a series expansion in temperature:

$$C_p = A + BT + CT^2 + DT^3 \quad (23-2)$$

where  $C_p$  = heat capacity of saturated liquid, cal/(g)(K);  $A, B, C, D$  = correlation constants for a chemical compound; and  $T$  = temperature, K.

A generalized least-squares computer program for minimizing deviation between collected data and calculated results was used to determine the correlation

constants. Average deviations are less than 1-3%.

Tabulated values are given in Table 23-II, where the temperature range is also provided. In most instances, the usable range covers the saturated liquid from its boiling point to temperatures above the boiling point, and in the general region (about 80-90% of  $T_c$ ) of the critical point. The results are not recommended for use in the immediate vicinity of the critical point (90-100% of  $T_c$ ). A comparison of calculated and collected data values is presented in Fig. 2 for a representative chemical, which in this case is ethanol.

*Example 23-2*—Estimate the heat capacity of benzene (C<sub>6</sub>H<sub>6</sub>) at 20°C. To solve this problem, substitute the correlation constants from Table 23-II:  $A = -1.481$ ;  $B = 15.46 \times 10^{-3}$ ;  $C = -43.70 \times 10^{-6}$ ; and  $D = 44.09 \times 10^{-9}$ ; and the temperature ( $T = 20^\circ\text{C} = 293.16\text{ K}$ ) into Eq. 23-2:

$$\begin{aligned}C_p &= -1.481 + 15.46 \times 10^{-3}(293.16) - 43.70 \times \\ &\quad 10^{-6}(293.16)^2 + 44.09 \times 10^{-9}(293.16)^3 \\ &= 0.406 \text{ cal/(g)(K)}\end{aligned}$$

## Correlation constants: heat capacity of liquid

Table 23-11

$$C_p = A + BT + CT^2 + DT^3$$

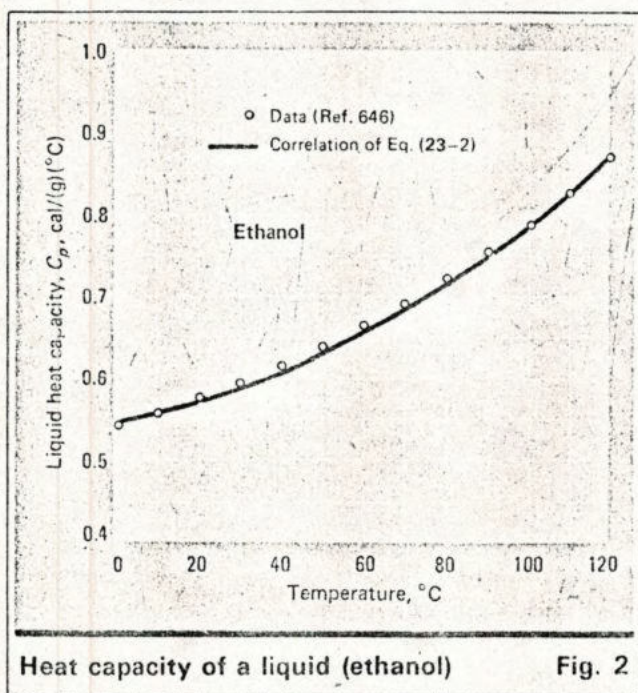
Compound	A	B x 10 <sup>3</sup>	C x 10 <sup>6</sup>	D x 10 <sup>9</sup>	C <sub>p</sub> at 25°C cal/(g)(°C)	Range, °C	References
<b>Halogens</b>							
Fluorine, F <sub>2</sub>	-0.268	252.8	-331.0	1.464	0.35 @ -183.1	-219 to -140.0	19,42,55,56
Chlorine, Cl <sub>2</sub>	-0.1322	4.720	-20.37	28.94	0.226 @ -34.06	-101 to 80	19,32,44,61,71
Bromine, Br <sub>2</sub>	-0.3925	4.452	-13.36	13.22	0.09	-7.2 to 280	4,19,43
Iodine, I <sub>2</sub>	-0.06263	51.87	-105.4	0.1247	0.075	113.6 to 500	4,19,43
<b>Sulfur oxides</b>							
Sulfur dioxide, SO <sub>2</sub>	-0.5737	10.34	-40.28	52.85	0.32 @ -10	-72.7 to 153	4,10,19,92
Sulfur trioxide, SO <sub>3</sub>	-3.973	40.16	-116.5	118.0	0.79	16.8 to 200	4,85,91
<b>Nitrogen oxides</b>							
Nitrous oxide, N <sub>2</sub> O	-2.915	44.24	-197.5	301.3	0.42 @ -89.5	-90.8 to 30	19,100
Nitric oxide, NO	-19.05	523.6	-4,704.5	14,217	0.61 @ -151.8	-163.8 to -135	19,106,116,134
Nitrogen dioxide, NO <sub>2</sub>	-1.625	16.99	-61.72	68.77	0.37 @ 21.2	-11.2 to 140	4,19,107,120
<b>Carbon oxides</b>							
Carbon monoxide, CO	0.5645	4.798	-143.7	911.95	0.515 @ -191.5	-205 to -150	12,14,19
Carbon dioxide, CO <sub>2</sub>	-19.30	254.6	-1,095.5	1,573.3	0.46 @ -30	-56.5 to 20	19,147,157
<b>Hydrogen halides</b>							
Hydrogen fluoride, HF	-1.414	20.41	-69.21	83.59	0.73 @ 19.5	-83.5 to 175	4,10,12,169,184
Hydrogen chloride, HCl	-0.1121	7.048	-35.31	66.21	0.405 @ -85.03	-114.2 to 20	12,18
Hydrogen bromide, HBr	-0.6353	10.02	-41.47	58.95	0.18 @ -66.8	-86.9 to 80	4,12
Hydrogen iodide, HI	-0.6418	7.739	-26.55	30.95	0.112 @ -35.5	-50.8 to 140	4,164
<b>Nitrogen hydrides</b>							
Ammonia, NH <sub>3</sub>	-1.923	31.1	-110.9	137.6	1.05 @ -33.43	-77.4 to 100	6,12,13,19,154
Hydrazine, N <sub>2</sub> H <sub>4</sub>	-4.634	49.00	-150.1	156.3	0.75	2 to 200	6,14,20,215,218
<b>Hydrogen oxides</b>							
Water, H <sub>2</sub> O	0.6741	2.825	-8.371	8.601	1.0	0 to 350	9,12,238,246
Hydrogen peroxide, H <sub>2</sub> O <sub>2</sub>	0.444	1.199	-2.738	2.615	0.63	-0.43 to 425	4,240,242,244,256,257,260
<b>Diatomic gases</b>							
Hydrogen, H <sub>2</sub>	3.79	-329.8	12,170.9	-2,434.8	2.1 @ -252.8	-253.4 to -245	19,47,284,293,302,306,307,311,321,333,335
Nitrogen, N <sub>2</sub>	-1.064	59.47	-768.7	3,257.3	0.49 @ -195.8	-209.9 to -160	19,43,47,300,306,321,325,331,332
Oxygen, O <sub>2</sub>	-0.4587	32.34	-395.1	1,575.7	0.405 @ -133.0	-218.4 to -130	19,47,300,303,306,321,334
<b>Inert gases</b>							
Helium, He	-1.733	1,386.0	-293,133.	27,280,000	0.96 @ -268.9	-270 to -268.5	10,47,345
Neon, Ne	-1.726	210.97	-6,982.4	79,375.0	0.44 @ -246	-248.7 to -230	10,43,47
Argon, Ar	-0.4778	23.17	-254.5	972.7	0.25 @ -185.9	-189.3 to -130	19,43,47
<b>Olefins</b>							
Ethylene, C <sub>2</sub> H <sub>4</sub>	-0.3402	6.218	-50.12	126.3	0.572 @ -103.7	-169 to -40	19,246,415,425,439,440
Propylene, C <sub>3</sub> H <sub>6</sub>	0.4706	1.683	-16.82	44.07	0.51 @ -47.7	-185.3 to 40	10,246,415,425,439,440
1-Butene, C <sub>4</sub> H <sub>8</sub>	0.5422	-1.179	3.409	2.195	0.515 @ -6.3	-185.4 to 80	10,246,415,425,441
<b>Alkanes</b>							
Methane, CH <sub>4</sub>	1.23	-10.33	72.0	-107.3	0.824 @ -161.5	-182.6 to -110	10,19,47,415,425,464
Ethane, C <sub>2</sub> H <sub>6</sub>	0.1368	8.481	-56.54	126.1	0.583 @ -88.2	-183.2 to 20	10,19,246,415,425,453
Propane, C <sub>3</sub> H <sub>8</sub>	0.3326	2.332	-13.36	30.16	0.532 @ -42.1	-187.7 to 80	10,19,246,415,425,463
<b>Xylenes</b>							
o-Xylene, C <sub>6</sub> H <sub>4</sub> (CH <sub>3</sub> ) <sub>2</sub>	-0.4408	6.892	-18.60	17.86	0.415	-25.2 to 325	9,413,488
m-Xylene, C <sub>6</sub> H <sub>4</sub> (CH <sub>3</sub> ) <sub>2</sub>	-0.03753	3.829	-10.71	11.46	0.40	-47.9 to 300	9,413,488
p-Xylene, C <sub>6</sub> H <sub>4</sub> (CH <sub>3</sub> ) <sub>2</sub>	-0.8429	8.961	-21.46	18.45	0.41	13.3 to 325	9,413,415,416,487,488
<b>Aromatics</b>							
Benzene, C <sub>6</sub> H <sub>6</sub>	-1.481	15.46	-43.70	44.09	0.41	5.53 to 250	3,19,415,481,503
Naphthalene, C <sub>10</sub> H <sub>8</sub>	-1.412	11.61	-25.26	19.63	0.42 @ 100	80.55 to 410	415,501,510
<b>Alkyl aromatics</b>							
Toluene, C <sub>6</sub> H <sub>5</sub> CH <sub>3</sub>	-0.1461	4.584	-13.46	14.25	0.395	-95 to 310	9,19,415,518
Ethylbenzene, C <sub>6</sub> H <sub>5</sub> C <sub>2</sub> H <sub>5</sub>	0.04941	2.711	-7.210	7.649	0.418	-95 to 320	9,415
Cumene, C <sub>6</sub> H <sub>5</sub> CH(CH <sub>3</sub> ) <sub>2</sub>	0.1201	2.457	-6.32	7.646	0.43	-96 to 340	15,343
<b>Benzene derivatives</b>							
Chlorobenzene, C <sub>6</sub> H <sub>5</sub> Cl	-0.1467	3.826	-10.66	10.41	0.31	-45.2 to 340	3,4,6,415,416,571,574
Aniline, C <sub>6</sub> H <sub>5</sub> NH <sub>2</sub>	0.1107	2.467	-6.085	5.927	0.49	-6.15 to 360	4,415,416,556,574
Phenol, C <sub>6</sub> H <sub>5</sub> OH	-0.6396	8.218	-18.42	14.47	0.535 @ 60	40.75 to 400	415,558,563,570,574
<b>Cycloalkanes</b>							
Cyclopropane, C <sub>3</sub> H <sub>6</sub>	-0.02613	6.913	-34.77	59.9	0.46 @ -32.8	-127.42 to 100	455,583,595
Cyclobutane, C <sub>4</sub> H <sub>8</sub>	-0.346	7.745	-27.0	33.42	0.445 @ 12.51	-90.73 to 190	594
Cyclopentane, C <sub>5</sub> H <sub>10</sub>	-0.02117	4.146	-13.16	15.95	0.41	-93.88 to 220	415,416,516,597
Cyclohexane, C <sub>6</sub> H <sub>12</sub>	-1.284	13.39	-35.1	32.27	0.43	6.55 to 260	415,416,503,546,577,601,603
<b>Olefin monomers</b>							
Isobutylene, C <sub>4</sub> H <sub>8</sub>	-0.1905	3.653	-16.79	28.92	0.525 @ -6.9	-140.35 to 125	10,415,514,607,513,619,627
Styrene, C <sub>6</sub> H <sub>5</sub> CH=CH <sub>2</sub>	-0.3154	5.465	-14.30	-14.34	0.41	-39.60 to 325	4,620,622,628
<b>Diolefins</b>							
1,3-Butadiene, C <sub>4</sub> H <sub>6</sub>	0.3735	1.049	-5.761	13.74	0.512 @ -4.41	-108.9 to 120	10,415,416,640,646
Isoprene, C <sub>5</sub> H <sub>8</sub>	0.1187	2.317	-9.033	13.66	0.405	-146 to 200	416,620,633,645
Chloroprene, C <sub>4</sub> H <sub>6</sub> Cl	0.0140	2.540	-8.839	11.20	0.315	-130 to 260	4,620

Correlation constants: heat capacity of liquid (continued)

Table 23-11

$$C_p = A + BT + CT^2 + DT^3$$

Compound	A	B x 10 <sup>3</sup>	C x 10 <sup>6</sup>	D x 10 <sup>9</sup>	C <sub>p</sub> at 25°C, cal/(g)(°C)	Range, °C	References
<b>Organic oxides</b>							
Ethylene oxide, C <sub>2</sub> H <sub>2</sub> O	0.2839	2.347	-11.66	20.04	0.47 @ 10.55	-112.5 to 180	4,659
Propylene oxide, C <sub>3</sub> H <sub>4</sub> O	0.1610	3.670	-15.48	22.94	0.495	-112 to 200	4,654,659
Butylene oxide, C <sub>4</sub> H <sub>6</sub> O	0.3182	2.037	-9.306	14.62	0.49	-150 to 240	14
<b>Primary alcohols</b>							
Methanol, CH <sub>3</sub> OH	0.8392	-3.231	8.296	-0.1689	0.608	-97.6 to 220	4,6,9,415,416,646,689,697,699,700,701
Ethanol, C <sub>2</sub> H <sub>5</sub> OH	-0.3499	9.559	-37.86	54.59	0.58	-114.1 to 180	4,6,19,415,416,646,692,693,700
n-Propanol, C <sub>3</sub> H <sub>7</sub> OH	-0.2761	8.573	-34.2	49.85	0.57	-126.2 to 200	4,6,415,416,692,698
n-Butanol, C <sub>4</sub> H <sub>9</sub> OH	-0.7587	12.97	-46.12	58.59	0.56	-89.3 to 200	4,6,415,692,697,700
<b>Chloromethanes</b>							
Methyl chloride, CH <sub>3</sub> Cl	0.04123	4.188	-19.11	29.73	0.358 @ -23.8	-97.5 to 120	4,19,646,709,717
Methylene chloride, CH <sub>2</sub> Cl <sub>2</sub>	0.01117	3.009	-11.43	14.97	0.285	-96.7 to 230	4,6,415,708,717,721
Chloroform, CHCl <sub>3</sub>	-0.09154	3.149	-10.64	12.4	0.225	-63.2 to 250	4,6,19,415,416,417,208,717,721
Carbon tetrachloride, CCl <sub>4</sub>	-0.01228	2.058	-7.04	8.610	0.20	-22.9 to 260	4,6,19,415,416,646,708,717,721



The calculated and data values compare favorably (0.406 versus 0.405).

*Example 23-3*—Estimate the energy required to heat toluene from 20°C to 100°C under saturation conditions. Recall from thermodynamics these conditions:

$$Q = \Delta H \approx \int_{T_1}^{T_2} C_p dT = \int_{T_1}^{T_2} (A + BT + CT^2 + DT^3) dT$$

$$= AT + \frac{BT^2}{2} + \frac{C}{3}(T^3) + \frac{D}{4}(T^4) \Big|_{T_1}^{T_2}$$

Substituting correlation constants  $A$ ,  $B$ ,  $C$  and  $D$  from Table 23-II, and temperatures  $T_1$  and  $T_2$  into the above equation yields:

$$\begin{aligned} \Delta H &= -(0.1461)(373.16 - 293.16) + \\ &\quad (4.584/2)(10^{-3})(373.16^2 - 293.16^2) - \\ &\quad (13.46/3)(10^{-6})(373.16^3 - 293.16^3) + \\ &\quad (14.25/4)(10^{-9})(373.16^4 - 293.16^4) \\ &= 33.04 \text{ cal/g} \end{aligned}$$

## DENSITIES OF LIQUIDS

*Praful N. Shah and Carl L. Yaws*

Liquid-density data are important in process engineering design, such as for the sizing of storage vessels that contain basic raw materials for a plant. In distillation, engineering design of condensers and reboilers requires knowledge of saturated liquid-density values for the column's overhead and bottom products. Additional usage is encountered in various heat, mass and momentum-transfer operations involving liquids.

### Correlation constants—Table 23-III

Saturated liquid densities, at any temperature, were

based on the following correlation:

$$\rho_L = AB^{-(1-T_r)^{2.7}} \quad (23-3)$$

where  $\rho_L$  = saturated liquid density, g/cm<sup>3</sup>;  $AB$  = correlation constants for a chemical compound; and  $T_r$  = reduced temperature,  $T/T_c$ .

Tabulated values for the correlation constants  $A$  and  $B$  are given in Table 23-3. The temperature range over which the correlation constants are valid covers the entire saturated liquid state, from the melting point to the critical point. A generalized least-squares computer



$$\rho_L = AB^{-(1-T_c/27)^{2/7}}, \text{ g/cm}^3$$

Compound	A	B	$T_c, ^\circ\text{C}$	$\rho$ at 25 $^\circ\text{C}$ , g/cm $^3$	Range, $^\circ\text{C}$	No. of data points	Average deviation, %	References
<b>Organic oxides</b>								
Ethylene oxide, $\text{C}_2\text{H}_4\text{O}$	0.3172	0.2608	195.3	0.86	-112.5 to 195.8	43	0.83	4,10,637
Propylene oxide, $\text{C}_3\text{H}_6\text{O}$	0.3123	0.2733	209.1	0.82	-112.0 to 209.1	6	0.04	4
Butylene oxide, $\text{C}_4\text{H}_8\text{O}$	0.2902	0.2649	252.6	0.83 @ 20.0	-150.0 to 252.6	2	0.01	4
<b>Primary alcohols</b>								
Methanol, $\text{CH}_3\text{OH}$	0.2928	0.2760	239.4	0.79	-97.6 to 239.4	71	1.14	4,415,484,637,646
Ethanol, $\text{C}_2\text{H}_5\text{OH}$	0.2903	0.2765	243.1	0.79	-114.1 to 243.1	103	1.35	4,415,484,637
n-Propanol, $\text{C}_3\text{H}_7\text{OH}$	0.2915	0.2758	263.6	0.80	-126.2 to 263.6	63	1.05	4,415,484,646
n-Butanol, $\text{C}_4\text{H}_9\text{OH}$	0.2633	0.2477	209.8	0.80	-89.3 to 289.3	25	1.60	4,415,484,646
<b>Chloromethanes</b>								
Methyl chloride, $\text{CH}_3\text{Cl}$	0.3542	0.2573	143.1	0.91	-97.7 to 143.1	87	0.85	9,637,708,712,710,733
Methylene chloride, $\text{CH}_2\text{Cl}_2$	0.3033	0.2141	241.0	1.32	-96.7 to 241.0	80	0.93	637,708,721,729,732,733
Chloroform, $\text{CHCl}_3$	0.5165	0.2666	263.4	1.48	-63.2 to 263.4	47	1.06	637,708,721,733,734
Carbon tetrachloride, $\text{CCl}_4$	0.5591	0.2736	283.2	1.58	-22.9 to 283.2	91	0.26	9,637,646,703,710,718,719,721

program (for minimizing deviations between calculated and data values) was effectively used to process the several thousand data points. The average deviation for all compounds tested is 0.55%.

If correlation constants are not available, one may make reasonable estimates of saturated liquid densities by letting  $A = \rho_c$ , and  $B = Z_c$  (critical compressibility factor). This method reduces the above correlation to the Rackett equation [489\*]. Application of this

\*Part 12 of this series, July 21, 1975, p. 122.

method to all compounds tested produced much greater deviations (average of 5%). Calculated and data values are compared in Fig. 23-3 for a representative chemical compound.

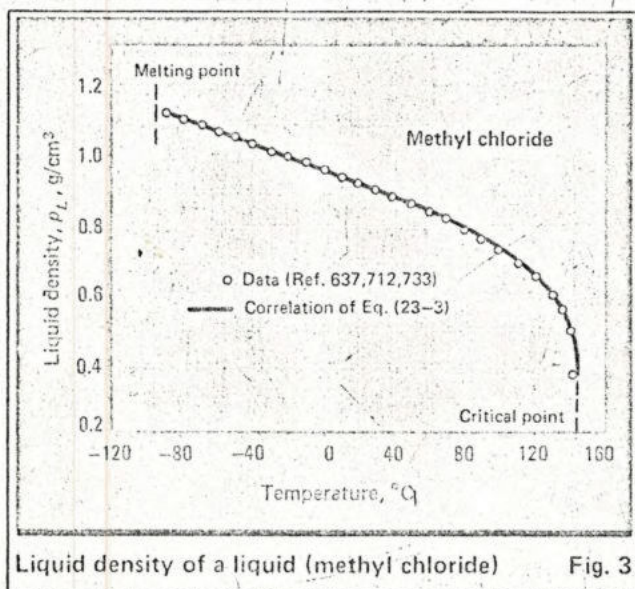
**Example 23-4**—Estimate the saturated liquid density of chlorobenzene ( $\text{C}_6\text{H}_5\text{Cl}$ ) at 50 $^\circ\text{C}$ . To solve this problem, substitute the correlation constants ( $A = 0.3706$ ;  $B = 0.2708$ ;  $T_c = 359.2^\circ\text{C} = 632.4\text{ K}$ ) from Table 23-3, and the temperature ( $T = 50^\circ\text{C} = 323.2\text{ K}$ ) into Eq. 23-3:

$$\begin{aligned}\rho_L &= AB^{-(1-T_c/27)^{2/7}} \\ &= (0.3706)(0.2708)^{-(1-(323.2/632.4))^{2/7}} \\ &= 1.075 \text{ g/cm}^3\end{aligned}$$

The calculated and data values compare favorably (1.075 versus 1.074).

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## THERMAL CONDUCTIVITIES OF LIQUIDS

Joseph W. Miller, Jr., James J. McGinley and Carl L. Yaws

Liquid thermal conductivity data are important in numerous chemical engineering applications that involve heat transfer. Representative examples include partial condensers handling liquids; total condensers for

the column-overhead product in a distillation operation; reboilers processing the column bottom in a distillation; liquid-phase reactors requiring heating or cooling; and general heat exchangers handling liquids.

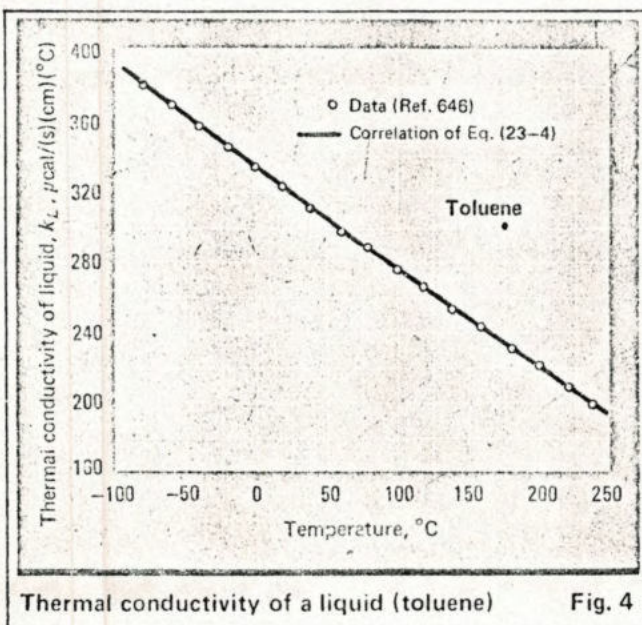
Correlation constants: thermal conductivity of liquids

Table 23-IV

Compound	$k_L = A + BT + CT^2$			$k_L$ at 20°C, (micro-cal)/(s)(cm)(°K)	Range, °C	References
	A	B x 10 <sup>2</sup>	C x 10 <sup>4</sup>			
<b>Halogens</b>						
Fluorine, F <sub>2</sub>	612.54	-162.29	-118.41	320 at -170.0	-219.0 to -140	14,65
Chlorine, Cl <sub>2</sub>	599.01	-48.30	-15.24	327	-101 to 132	14,65
Bromine, Br <sub>2</sub>	384.05	-3.07	-8.04	300	-7.2 to 300	14,63,65
Iodine, I <sub>2</sub>	320.12	10.26	-4.85	275 at 156	113 to 512	14,65
<b>Sulfur oxides</b>						
Sulfur dioxide, SO <sub>2</sub>	2,140.81	-783.66	71.43	458	-50 to 150	93
Sulfur trioxide, SO <sub>3</sub>	2271.20	-760.56	66.60	615	10 to 210	743
<b>Nitrogen oxides</b>						
Nitrous oxide, N <sub>2</sub> O	846.95	-213.80	-4.29	120	-102 to 20	14,125,126
Nitric oxide, NO	423.34	253.19	-212.35	438 at -160	-163 to -96	14,65
Nitrogen dioxide, NO <sub>2</sub>	519.74	6.22	-25.73	317	-11 to 142	14,19
<b>Carbon oxides</b>						
Carbon monoxide, CO	475.48	3.31	-214.26	360 at -200	-205 to -145	14,19,65
Carbon dioxide, CO <sub>2</sub>	972.06	-201.53	-22.99	184	-56 to 26	14,19,142,151,152
<b>Hydrogen halides</b>						
Hydrogen fluoride, HF	1,695.67	-205.91	-15.38	950	-83 to 165	13,14,65
Hydrogen chloride, HCl	1,071.70	-18.44	-65.81	453	-114 to 31	14,65,173,175,176
Hydrogen bromide, HBr	579.89	38.34	-41.11	339	-87 to 70	14,65,173
Hydrogen iodide, HI	620.79	-10.27	-21.73	404	-50 to 110	14,65,173
<b>Nitrogen hydrides</b>						
Ammonia, NH <sub>3</sub>	2,551.30	-376.62	-29.35	1,196	-77 to 100	13,14,19,207
Hydrazine, N <sub>2</sub> H <sub>4</sub>	2,859.98	-175.23	-24.16	2,139	2 to 318	13,14
<b>Hydrogen oxides</b>						
Water, H <sub>2</sub> O	-916.62	1,251.73	-152.12	1,452	0 to 350	4,13,14,19,238,246,258
Hydrogen peroxide, H <sub>2</sub> O <sub>2</sub>	-466.56	805.86	-87.58	1,143	0 to 400	13,14,258
<b>Diatomic gases</b>						
Hydrogen, H <sub>2</sub>	-20.41	2,473.70	-5,347.26	268 @ -250	-259 to -241	19,47,272,287,290,293,298,304,307,317,333
Nitrogen, N <sub>2</sub>	627.99	-368.91	-22.57	275 @ -182.5	-209 to -152	19,47,65,288,290,299,300,303,306,316,317,328,332
Oxygen, O <sub>2</sub>	583.79	-210.49	-48.31	355 @ -183	-218 to -135	19,47,65,288,300,317,327,334
<b>Inert gases</b>						
Helium, He	-954.21	1.55 · 10 <sup>5</sup>	-5.0 · 10 <sup>6</sup>	200 @ -271.3	-271.3 to -271.0	19,44,47,290,345,364,374,392,399
	93.35	-4,376.85	9.05 · 10 <sup>4</sup>	50 @ -270.0	-271.0 to -268.3	
Neon, Ne	32.82	2,004.4	-4,121.7	240 @ -239.5	-248.7 to -229.5	19,43,44,290,374,392
Argon, Ar	444.63	-98.43	-85.71	260 @ -173	-189.3 to -128.0	19,43,44,47,288,290,306,316,328,345,374,392,402
<b>Olefins</b>						
Ethylene, C <sub>2</sub> H <sub>4</sub>	851.45	-228.94	-4.71	351 @ -63	-169.2 to -4.0	14,19,84,246,421,440
Propylene, C <sub>3</sub> H <sub>6</sub>	694.04	-144.57	0.30	275	-185 to 70	14,246,422,426,430,440
1 Butene, C <sub>4</sub> H <sub>8</sub>	609.89	-95.16	-2.71	312	-185 to 120	14,246
<b>Alkanes</b>						
Methane, CH <sub>4</sub>	722.72	-144.42	-76.36	325 @ -120	-182.6 to -80.0	19,47,288,459,464
Ethane, C <sub>2</sub> H <sub>6</sub>	693.31	-165.88	-4.87	170	-183.2 to 20	208,444
Propane, C <sub>3</sub> H <sub>8</sub>	623.51	-126.79	-2.12	234	-187.7 to 80.0	268,445
<b>Xylenes</b>						
o-Xylene, C <sub>6</sub> H <sub>4</sub> (CH <sub>3</sub> ) <sub>2</sub>	393.83	-17.77	-3.38	313	-25.2 to 332.0	6,9,109,413,481,486
m-Xylene, C <sub>6</sub> H <sub>4</sub> (CH <sub>3</sub> ) <sub>2</sub>	392.29	-3.50	-5.70	333	-47.9 to 330.0	6,9,409,413,470,471,481,482,483,436
p-Xylene, C <sub>6</sub> H <sub>4</sub> (CH <sub>3</sub> ) <sub>2</sub>	355.0	6.49	-6.74	316	13.3 to 336.0	475,481,483
<b>Aromatics</b>						
Benzene, C <sub>6</sub> H <sub>6</sub>	424.26	1.14	-9.03	350	5.53 to 760	14,19,443,481,484,492,493,494,514
Naphthalene, C <sub>10</sub> H <sub>8</sub>	317.24	14.22	-4.04	311 at 120°	80.55 to 460.0	443,496
<b>Alkyl aromatics</b>						
Toluene, C <sub>6</sub> H <sub>5</sub> CH <sub>3</sub>	485.10	-53.84	-0.59	322	-95 to 308	9,14,19,288,409,470,471,475,481,482,483,486,489,516,525,526,527,528,530,531
Ethylbenzene, C <sub>6</sub> H <sub>5</sub> C <sub>2</sub> H <sub>5</sub>	511.66	-82.15	4.64	311	-95 to 300	14,481,516,535,539
Cumene, C <sub>6</sub> H <sub>5</sub> CH(CH <sub>3</sub> ) <sub>2</sub>	471.26	-57.82	0.49	306	-96 to 305	14,483,486,516,532,546
<b>Benzene derivatives</b>						
Chlorobenzene, C <sub>6</sub> H <sub>5</sub> Cl	432.04	-38.31	-1.12	310	-45.2 to 330	14,409,413,416,481,484,486,535,539,546,551,552,559,562,565,566,567,568,572
Aniline, C <sub>6</sub> H <sub>5</sub> NH <sub>2</sub>	537.55	-30.42	-1.49	436	-6.15 to 408	4,14,409,413,416,481,484,486,535,539,546,551,552,559,562,565,566,568,572
Phenol, C <sub>6</sub> H <sub>5</sub> OH	440.93	86.70	-7.01	400 at 222°C	40.75 to 395	14
<b>Cycloalkanes</b>						
Cyclopropane, C <sub>3</sub> H <sub>6</sub>	396.82	-42.10	-6.72	216	-127.42 to 117.0	431
Cyclobutane, C <sub>4</sub> H <sub>8</sub>	316.67	-29.07	-3.62	230	-90.73 to 162.0	431
Cyclopentane, C <sub>5</sub> H <sub>10</sub>	511.73	-61.80	-1.39	319	-93.88 to 215.0	14,481,539,606
Cyclohexane, C <sub>6</sub> H <sub>12</sub>	388.26	-22.72	-3.30	293	6.55 to 254.0	14,481,486,496,539,566,605,606
<b>Olefin monomers</b>						
Isobutylene, C <sub>4</sub> H <sub>8</sub>	555.29	-124.28	6.23	245	-140.35 to 100.0	14,481
Styrene, C <sub>6</sub> H <sub>5</sub> CH=CH <sub>2</sub>	613.97	-80.82	0.40	411	-30.6 to 350	14,481



Compound	$k_L = A + BT + CT^2$			$k_L$ at 20°C, (micro-cal)/(s)(cm)(°K)	Range, °C	References
	A	B × 10 <sup>2</sup>	C × 10 <sup>4</sup>			
<b>Diolefins</b>						
1,3-Butadiene, C <sub>4</sub> H <sub>6</sub>	718.26	-187.18	11.74	268	-108.9 to 120.0	481
Isoprene, C <sub>5</sub> H <sub>8</sub>	523.95	-75.70	-1.37	290	-146 to 160	445,646
Chloroprene, C <sub>4</sub> H <sub>5</sub> Cl	459.65	-82.14	3.56	252	-130 to 220	481
<b>Oxigene oxides</b>						
Ethylene oxide, C <sub>2</sub> H <sub>4</sub> O	626.62	-79.51	-2.85	369	-112.50 to 180	14,481
Propylene oxide, C <sub>3</sub> H <sub>6</sub> O	563.51	-53.40	-5.08	363	-112 to 180	14,481
Butylene oxide, C <sub>4</sub> H <sub>8</sub> O	512.56	-23.56	-7.30	366	-150 to 240	14,481
<b>Primary alcohols</b>						
Methanol, CH <sub>3</sub> OH	770.13	-114.23	2.79	459.2	-97.6 to 210.0	6,9,14,19,416,475,486,562,637,646,674,680,684,695,686,690,694
Ethanol, C <sub>2</sub> H <sub>5</sub> OH	628.0	-91.88	5.28	404	-114.1 to 180	6,9,14,19,416,475,484,846,537,562,639,646,674,680,684,685,686,690,694
n-Propanol, C <sub>3</sub> H <sub>7</sub> OH	442.74	-8.04	-5.29	368	-126.2 to 220	9,14,465,486,562,637,646,660,684,685,686,690,694,704
n-Butanol, C <sub>4</sub> H <sub>9</sub> OH	546.51	-64.42	0.316	361	-89.3 to 230.0	6,14,416,475,484,486,561,637,646,668,680,684,685,686,690,694
<b>Chloromethanes</b>						
Methyl chloride, CH <sub>3</sub> Cl	902.96	-158.57	-4.21	402	-97.7 to 123.0	19,637,708,717
Methylene chloride, CH <sub>2</sub> Cl <sub>2</sub>	537.74	-60.47	-2.69	338	-96.7 to 186.0	481,637,708,717
Chloroform, CHCl <sub>3</sub>	390.25	-20.58	-5.06	287	-63.2 to 237.0	9,19,481,532,637,708,717
Carbon tetrachloride, CCl <sub>4</sub>	383.95	-45.45	-0.24	249	-22.9 to 224.0	9,19,475,481,532,540,637,646,707,708,717



### Correlation constants—Table 23-IV

The thermal conductivity of a saturated liquid was correlated as a function of temperature by the relation:

$$k_L = A + BT + CT^2 \quad (23-4)$$

where  $k_L$  = thermal conductivity of saturated liquid, microcal/[(s)(cm)(K)];  $A, B, C$  = correlation constants for a chemical compound; and  $T$  = temperature, K.

Deviations between data and calculated results were minimized by using a generalized least-squares computer program to determine the correlation constants.

Average deviations in most cases are less than 2.5%.

The correlation constants are presented in Table 23-IV. The usable temperature range covers the saturated liquid-phase from the melting point to temperatures above the boiling point, and in the region 80-90% of  $T_c$  of the critical point. The results are not recommended in the immediate vicinity of the critical point (90-100% of  $T_c$ ). Correlation and data values are compared in Fig. 23-4 for a representative chemical.

**Example 23-5**—Estimate the thermal conductivity of liquid toluene (C<sub>6</sub>H<sub>5</sub>CH<sub>3</sub>) at 150°C. To solve this problem, substitute the correlation constants ( $A = 485.1$ ;  $B = -53.8 \times 10^{-2}$ ;  $C = -0.59 \times 10^{-4}$ ) from Table 23-IV, and the temperature ( $T = 150^\circ\text{C} = 423.16\text{ K}$ ) into Eq. 23-4:

$$\begin{aligned} k_L &= A + BT + CT^2 \\ &= 485.1 - (53.84)(10^{-2})(423.16) - \\ &\quad (0.59)(10^{-4})(423.16)^2 \\ &= 247 \text{ microcal}/(\text{s})(\text{cm})(\text{K}) \end{aligned}$$

The calculated and data values compare favorably (247 versus 249).

### The authors

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Biographical sketches for Joseph W. Miller, Jr., Gordon R. Schorr and Carl L. Yaws appeared in the Aug. 16 issue, p. 87, 1976. J. W. Miller was formerly a process engineer with E. I. du Pont de Nemours & Co.